

**15G-101**  
**May-2015**  
**B.Sc., Sem.-II**  
**Core Course-3 : Statistics**  
**Paper-103**  
**(Basic Probability Theory-I)**

**Time : 3 Hours]**

**[Max. Marks : 70**

- Instructions :** (1) All questions carry equal marks.  
(2) Scientific calculator is allowed.

1. (a) Explain various measures of dispersion along with their merits and demerits. 7

**OR**

Write a short note on skewness and kurtosis.

- (b) Define moments. Establish relation between first four row moments and central moments. 7

**OR**

The first four moments about the value 4 of a variable are  $-1.5$ ,  $17$ ,  $-30$  and  $108$ . Find moments about mean,  $\beta_1$  and  $\beta_2$ .

2. (a) (i) State and prove Baye's theorem. 7  
(ii) Define conditional probability and in usual notations prove that  $P(A \cap B) = P(A) \cdot P(A/B)$ .

**OR**

An urn contains 5 white and 5 black balls. 4 balls are drawn from these urn and put into another urn. From the second urn a ball is drawn and is found to be white. What is the probability of drawing a white ball again at the next draw ?

- (b) Ravi speaks truth 4 out of 5 times. He tossed a die and reports that there is a six. What is the chance that actually there was six ? 7

**OR**

There are 10 urns of which each of 3 contains 1 white and 9 black balls, each of other 3 contains 9 white and 1 black ball and of the remaining 4 each contains 5 white and 5 black balls. One of the urn is selected at random and a ball taken blindly from it turns out to be white. What is the probability that an urn containing 1 white and 9 black balls was selected ?

3. (a) Explain various components of time series and show their importance by taking few illustrations. 7

**OR**

Describe the method of least squares for measuring secular trends in time series. Also explain the procedure for fitting 2<sup>nd</sup> degree parabola by the method of least square.

- (b) Explain the method of moving averages for measuring the trend. 7

**OR**

What do you mean by seasonal indices in time series ? What are the various methods of determining seasonal indices ? Explain any one of them.

4. (a) What are the different steps in the process of decision making ? Define the following terms : 7

- (i) State of Nature (ii) Strategy  
 (iii) Pay-off Matrix.

**OR**

Explain the following :

- (i) Maxi-min principle (ii) Horwich's principle  
 (iii) Laplace's principle

- (b) Find the best act by using EMV principle for the following payoff matrix : 7

Event	Probability	Act			
		A	B	C	D
S <sub>1</sub>	0.40	15	50	10	15
S <sub>2</sub>	0.30	20	15	50	10
S <sub>3</sub>	0.20	40	20	15	50
S <sub>4</sub>	0.10	60	40	20	15

**OR**

Determine the best act for the following pay-off matrix by applying :

- (i) Maxi-min principle  
 (ii) Maxi-max principle  
 (iii) Horwich's principle (with  $\alpha = 0.4$ )  
 (iv) Laplace principle

Event	Act			
	A	B	C	D
S <sub>1</sub>	10	6	3	-2
S <sub>2</sub>	5	-2	4	8
S <sub>3</sub>	-3	7	-1	6

5. Write answers in brief :

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- (i) The marks (out of 50) obtained by two students in three subjects are Student A : 25, 30, 5; Student B : 20, 20, 22. Which student's marks shows greater variability ? Justify.
  - (ii) Why Range is not the best measure of dispersion ?
  - (iii) Which component of time series is mainly applicable in the following cases ?
    - (1) Fire in a factory
    - (2) Sales of new year greeting cards.
  - (iv) Give the limitation of method of moving average.
  - (v) Give the condition of independence of two events A and B in terms of probability.
  - (vi) Define EMV and EVPI.
  - (vii) Give the relation between EMV and EVPI.
  - (viii) Define central moments.
  - (ix) Give the formula for Karl Pearson's coefficient of skewness.
  - (x) Define EOL.
  - (xi) Standard deviation is the best measure of dispersion – Justify.
  - (xii) What is the usage of coefficient of variation ?
  - (xiii) If  $\beta_1 = 1$  and  $\beta_2 = 4$ , comment upon the nature of the distribution.
  - (xiv) How cyclical variations differ from seasonal variations ?
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