

## IM.Sc. (AIML) (NEP) Sem.-4 Examination

DSC-C-AIML-241-T

Adv. Statistics for M.L.

Time : 2-00 Hours]

April-2025

[Max. Marks : 50

- ❖ Read all questions carefully before attempting to answer.
- ❖ This question paper contains 05 questions.
- ❖ You may use a scientific calculator.
- ❖ All answers must be written neatly and legibly.
- ❖ Attempt all questions.

Q-1 (A) Explain type – I and type – II error [04]

Q-1 (B) A mobile company claims that the average battery life of their phone is 100 hours. A sample of 25 phones had a mean battery life of 105 hours with a standard deviation of 10 hours. Test the company's claim using a t-test at 5% significance level. (Given  $t_{0.05} = 2.064$ ) [06]

OR

Q-1 (A) Explain the terms [04]

- (1) Level of Significance
- (2) Parameter and Statistics
- (3) Degree of Freedom
- (4) Confidence Interval

Q-1 (B) Ten individuals' weights (in kg) before and after a 4-week diet. Test whether the diet had a significant effect at 5% level. (Given  $t_{0.05} = 2.262$ ) [06]

| Person | 1  | 2  | 3  | 4   | 5  | 6  | 7  | 8  | 9  | 10 |
|--------|----|----|----|-----|----|----|----|----|----|----|
| Before | 85 | 90 | 95 | 100 | 88 | 92 | 87 | 91 | 89 | 86 |
| After  | 82 | 87 | 91 | 96  | 84 | 89 | 83 | 88 | 85 | 82 |

Q-2 (A) Explain Wilcoxon sign rank test [04]

Q-2 (B) A group of 8 individuals performed stretching exercises for 3 months. The heights (in cm) of the individuals before and after the exercise program were recorded. Test if there was a significant increase in height at the 5% level. Use sign test. [06]

| Person      | 1   | 2   | 3   | 4   | 5   | 6   | 7   | 8   |
|-------------|-----|-----|-----|-----|-----|-----|-----|-----|
| Before (cm) | 170 | 160 | 165 | 172 | 168 | 174 | 169 | 162 |
| After (cm)  | 171 | 161 | 166 | 173 | 169 | 175 | 170 | 163 |

**OR**

Q-2 (A) Explain sign test [04]

Q-2 (B) A car mechanic wants to check if tuning improved fuel efficiency (in km/l). Use Wilcoxon sign rank test. [06]

| Car    | 1    | 2    | 3    | 4    | 5    | 6    |
|--------|------|------|------|------|------|------|
| Before | 15.2 | 14.8 | 15   | 15.6 | 14.9 | 15.1 |
| After  | 16.1 | 15.5 | 15.8 | 16.3 | 15.7 | 15.9 |

Q-3 (A) Explain F -test [04]

Q-3 (B) Exam Scores from Different Teaching Methods are determined. Test the variability at 5% level of significance (Given  $F_{0.05} = 4.26$ ) [06]

| Method 1 | Method 2 | Method 3 |
|----------|----------|----------|
| 75       | 82       | 79       |
| 78       | 84       | 81       |
| 74       | 80       | 77       |
| 76       | 83       | 80       |

**OR**

Q-3 (A) Explain one-way ANOVA [04]

Q-3 (B) Test the variabilities between the operators and machines at 5% level of significance. (Given  $F_{0.05} = 2.5$ ) [06]

| Machines | Operate A | Operate B | Operate C |
|----------|-----------|-----------|-----------|
| I        | 7         | 2         | 9         |
| II       | 7         | 4         | 8         |
| III      | 4         | 8         | 7         |
| IV       | 6         | 3         | 8         |

Q-4 (A) Why there are two regression lines [04]

Q-4 (B) Find regression lines and estimate x when y is 100 [06]

|   |     |     |     |     |    |
|---|-----|-----|-----|-----|----|
| X | 102 | 103 | 103 | 107 | 99 |
| Y | 104 | 98  | 89  | 79  | 97 |

**OR**

Q-4 (A) Give properties of Regression Co-efficient [04]

Q-4 (B) Find regression lines and estimate y when x is 34 [06]

|   |    |    |    |    |    |    |
|---|----|----|----|----|----|----|
| X | 37 | 36 | 35 | 32 | 31 | 30 |
| Y | 30 | 39 | 35 | 38 | 31 | 38 |

Q-5 Answer the followings (Any Ten) [10]

- Which of the following best describes the slope in a simple linear regression model?
  - The predicted value of y when  $x = 0$ .
  - The change in y for a one-unit increase in x.
  - The intercept on the y-axis.
  - The correlation between x and y.

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2. The coefficient of determination ( $R^2$ ) in regression analysis represents:
  - A) The variance in x explained by y.
  - B) The proportion of variance in y explained by x.
  - C) The slope of the regression line.
  - D) The standard error of the regression.
  
3. Which assumption of the linear regression model states that the variance of the residuals is constant across all levels of x?
  - A) Linearity
  - B) Independence
  - C) Homoscedasticity
  - D) Normality
  
4. A one-sample t-test is used to test whether:
  - A) Two independent groups have the same mean.
  - B) The mean of a single sample is equal to a hypothesized value.
  - C) The variances of two samples are equal.
  - D) Two paired samples differ significantly.
  
5. The paired t-test is most appropriately used when:
  - A) Comparing two independent groups' means.
  - B) Comparing measurements on the same subjects before and after an intervention.
  - C) Comparing variances of two samples.
  - D) Assessing the correlation between two continuous variables.
  
6. In a paired t-test, the test is performed on the differences between paired observations. The null hypothesis is that the mean difference is:
  - A) Greater than zero.
  - B) Less than zero.
  - C) Equal to zero.
  - D) Not equal to zero.
  
7. If a paired t-test yields a p-value of 0.03, and the significance level is 0.05, you should:
  - A) Fail to reject the null hypothesis.
  - B) Reject the null hypothesis.
  - C) Accept the null hypothesis.
  - D) Increase the sample size.
  
8. The Chi-Square test is most appropriately used for:
  - A) Testing the difference in means between two groups.
  - B) Testing the association between two categorical variables.
  - C) Comparing a sample mean to a population mean.
  - D) Evaluating the correlation between two continuous variables.

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9. In a Chi-Square test for independence, the expected frequency for a cell in a contingency table is calculated as:
- A)  $(\text{Row total} + \text{Column total}) / \text{Grand total}$
  - B)  $(\text{Row total} \times \text{Column total}) / \text{Grand total}$
  - C)  $(\text{Row total} - \text{Column total}) / \text{Grand total}$
  - D)  $(\text{Row total} \div \text{Column total}) \times \text{Grand total}$
10. The Wilcoxon Signed-Rank Test is used when the assumptions of the parametric paired t-test are violated, particularly when the differences are:
- A) Normally distributed.
  - B) Not normally distributed.
  - C) Categorical.
  - D) Homoscedastic.
11. The null hypothesis in a Wilcoxon Signed-Rank Test states that:
- A) The mean difference is zero.
  - B) The median difference is zero.
  - C) The variance of the differences is equal to one.
  - D) The sum of the ranks is zero.
12. In a sign test, observations with differences equal to zero are:
- A) Counted as positive.
  - B) Counted as negative.
  - C) Ignored.
  - D) Doubled in the analysis.

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