

B.Sc Sem.-6 (Rep) Examination

CC 307

Statistics

September-2024

Time : 2-30 Hours]

[Max. Marks : 70]

Instructions

1. All questions are compulsory and carry equal marks.
2. Figures to the right indicate full marks of the questions/sub-questions.

Q-1 (a) Define terms: Statistical hypothesis, Simple and composite (07) hypothesis, critical region, type I and Type – II errors, level of significance.

(b) When a balanced die is tossed, p be the probability that it shows (07) an even number. It is desired to test the hypothesis that $H_0: p = \frac{1}{2}$ vs $H_1: p = \frac{1}{3}$. For this a procedure is given below:

Toss the die twice and accept H_0 if both times it shows even number. Find probabilities of Type – I and Type – II errors and also find power of the test.

OR

Q-1 (a) Define Most Powerful Critical Region and Most Powerful Test. (07) Hence or otherwise, State and prove Neyman Pearson Lemma.

(b) A random sample of size n is taken from $Ber(1, \theta)$, Use Neyman (07) Pearson Lemma to find out most powerful critical region for testing $H_0: \theta = \theta_0$ Vs $H_1: \theta = \theta_1$, (Where $\theta_0 > \theta_1$).

Q-2 (a) Explain the test procedure to test the significance of difference (07) between two means, based on two large samples.

(b) Derive test statistic for testing the null hypothesis $H_0: \rho = 0$. (07)

OR

Q-2 (a) Explain test procedure of testing significance of difference (07) between two population means.

(b) Given a single observed correlation coefficients r based on a (07) bivariate random sample of size n , then discuss a test procedure of testing significance of single observed correlation correlation. Also, find $100(1-\alpha)\%$ confidence Interval for ρ .

Q-3 (a) Derive a test statistic for testing hypothesis independence of two (07) attributes.

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(b) State applications of t – distribution. (07)
 Derive test statistic to test null hypothesis $H_0: r_{12.3} = 0$.

OR

Q-3 (a) Explain test procedure to test null hypothesis $H_0: p_1 = p_2$ against (07) alternative hypothesis $H_1: p_1 < p_2$ (07)
 (b) Explain variance ratio test, in details. (07)

Q-4 (a) What are nonparametric tests? (07)
 Describe test procedure of large sample sign test.
 (b) Explain in detail Mann Whitney test. (07)

OR

Q-4 (a) What is median test? (07)
 (b) State differences between parametric and nonparametric tests. (07)

Q-5 Answer the following Questions. (14)

- i) What is type II error?,
- ii) Define Uniformly Most powerful critical region.
- iii) What is power of the test.?
- iv) A probability distribution of a test statistic defined on a large sample, is approximately normal. Do you agree?
- v) Select an appropriate option from (i) and (ii) for the following:
 In paired t – test, difference is
 (i) $d = x - y$ (ii) $d = \bar{x} - \bar{y}$
- vi) State the variance of a distribution of a test statistic, used for testing an observed partial correlation coefficient.
- vii) Which distribution is useful in deriving a test statistic for testing significance of observed multiple correlation coefficient.
- viii) Give a value of test statistic to test $H_0: \sigma = \sigma_0$
- ix) Define null and alternate hypotheses.
- x) Give one limitation of nonparametric test.
- xi) State situation, in which median test is useful.
- xii) Define RUN.
- xiii) State one assumption associated with nonparametric test.
- xiv) With respect to Test of hypothesis, out of two types of errors, which one is more serious?

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