

MSc IT DMVI Sem-3 Examination

DMVIBSC-17

Mathematical Foundation of Computer Science

Time : 2-30 Hours]

December-2024

[Max. Marks : 70

Instructions:

- Figures to the right indicate Full Marks.
- Do not write anything on the question paper.
- Simple calculator is allowed. Do not use a scientific calculator.

Question:1 Choice the correct answer:

[14]

[1]

Find the determinant of matrix $\begin{bmatrix} 2 & 3 \\ 4 & 5 \end{bmatrix}$

(A)-2

(B)3

(C)4

(D)-5

2

If a matrix has 5 rows and 1 column, it is called?

(A)Row matrix

(B) square matrix

(C)Column matrix

(D)Null matrix

3

Which of the following is a square matrix?

(A)A matrix with 3 rows and 2 columns

(B) A matrix with 4 rows and 4 columns

(C) A matrix with 2 rows and 3 columns

(D) A matrix with 1 row and 4 columns

(P.T.O)

- 4 A matrix in which all the diagonal elements are one is called?
- (A) diagonal matrix
 - (B) Scalar matrix
 - (C) Null matrix
 - (D) Identity matrix
- 5 A matrix with only one row is called?
- (A) Row matrix
 - (B) Column matrix
 - (C) square matrix
 - (D) Diagonal matrix
- 6 The output of an AND gate is 1 when
- (A) At least one input is 1
 - (B) All inputs are 1
 - (C) All inputs are 0
 - (D) At least one input is 0
- 7 What is the output of a NOR gate if both inputs are 1?
- (A) 0
 - (B) 1
 - (C) Depends on the third input
 - (D) Indeterminate
- 8 Which gate's output is always 0 when all inputs are 1?
- (A) NOR
 - (B) NAND
 - (C) XOR
 - (D) AND
- 9 a matrix with 3 rows and 3 columns is called
- (A) square matrix
 - (B) row matrix
 - (C) column matrix
 - (D) null matrix
- 10 a matrix which satisfy $A = A^T$ is called:
- (A) idempotent matrix
 - (B) involutory matrix
 - (C) nilpotent matrix
 - (D) symmetric matrix

- 11 a matrix which satisfies $A^2 = A$ is called?
 (A) Idempotent matrix
 (B) Involutory matrix
 (C) Nilpotent matrix
 (D) Symmetric matrix
- 12 a matrix with 5 rows and 4 columns is called?
 (A) rectangular matrix
 (B) Square matrix
 (C) row matrix
 (D) column matrix
- 13 a matrix which satisfy $A^3 = 0$ is called?
 (A) Idempotent matrix
 (B) Involutory matrix
 (C) Nilpotent matrix
 (D) Symmetric matrix
- 14 a matrix in which all the elements are zero is called ?
 (A) Unit matrix
 (B) Scalar matrix
 (C) null matrix
 (D) Identity matrix

- Question:2 Answer the following question [14]
- [A] Let $A = \{1, 2, 3\}$, $B = \{3, 4, 5\}$, $C = \{2, 3, 6\}$. Find [07]
 i. $A \cup B \cap C$
 ii. $A - B \cup C$.
- [B] Simplify the following Boolean expression: [07]
 $(A + B')(A' + C)$.

(P.T.O)

Question:3 Answer the following question [14]

[A] Write the truth table for $(P \wedge Q) \vee (\neg P \vee \neg Q)$ [07]

[B] Prove that $\sqrt{2}$ is an irrational number using proof by contradiction. [07]

Question: 4 Answer the following question. [14]

[A] Find determinant of given matrix: [07]

$$X = \begin{bmatrix} 2 & 6 & 0 \\ 5 & 2 & -2 \\ 6 & 4 & 0 \end{bmatrix}$$

OR

Find determinant of given matrix:

$$X = \begin{bmatrix} 2 & 1 & 3 \\ 5 & 6 & 2 \\ 1 & 5 & 0 \end{bmatrix}$$

[B] Find inverse of given matrix by row elementary method: [07]

$$A = \begin{bmatrix} 1 & 1 & 2 \\ 2 & -1 & 0 \\ 2 & 2 & 1 \end{bmatrix}$$

OR

Find inverse of given matrix by row elementary method:

$$A = \begin{bmatrix} 3 & 0 & 2 \\ 2 & 0 & -2 \\ 0 & 1 & 1 \end{bmatrix}$$

Question: 5 Answer the following question. [14]

[A] Find values of given system of linear equation by Cramer's rule [07]

$$x + y + z = 2$$

$$2x + y + 3z = 9$$

$$x - 3y + z = 10$$

OR

Find values of given system of linear equation by Cramer's rule

$$2x + 3y - 5z = 1$$

$$x + y - z = 2$$

$$2y + z = 8$$

[B]

Find values of given system of linear equation by Jordan method: [07]

$$x + 2y + 4z = 8$$

$$2x + 3y + 5z = 10$$

$$3x + 2y + 6z = 15$$

OR

Find values of given system of linear equation by Jordan method:

$$x + y + z = 9$$

$$2x - 3y + 4z = 13$$

$$3x + 4y + 5z = 40$$
