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# MD-107 

March-2019

# B.B.A., Sem.-V <br> CC-304 : Operations Research \& Quantitative Techniques 

Time : 2:30 Hours]
[Max. Marks : 70
Instructions : (1) Graph paper will be supplied on request.
(2) Use of simple calculator is allowed.

1. (a) (i) What is Linear Programming ? Give tis mathematical formulation.
(ii) Use the graphical method to solve the following linear programming problem.

Maximize $\quad Z=15 x+10 y$
Subject to the constraints

$$
\begin{aligned}
& 4 x+6 y \leq 360 \\
& 3 x+0 y \leq 180 \\
& 0 x+5 y \leq 200 \\
& x, y \geq 0
\end{aligned}
$$

## OR

(i) Define O.R. Give applications of O.R. in various fields.
(ii) A manufacturer produces two different models : X and Y of the same product. Model X makes a contribution of ₹ 50 per unit and model Y, ₹ 30 per unit towards total profit. Raw materials $r_{1}$ and $r_{2}$ are required for production. At least 18 kg of $\mathrm{r}_{1}$ and 12 kg of $\mathrm{r}_{2}$ must be used daily. Also at most 34 hours of labour are to be utilized. A quantity of 2 kg of $\mathrm{r}_{1}$ is needed for model $X$ and 1 kg of $r_{1}$ for model Y. For each of $X$ and $Y, 1 \mathrm{~kg}$ of $r_{2}$ is required. It takes 3 hours to manufacture model $X$ and 2 hours to manufacture model Y. How many units of each model should be produced to maximize the profit?

Solve by graphical method
(b) Answer the following: (any four)
(i) Define Feasible solution.
(ii) Linear programming is a branch of mathematical programming.
(True/False)
(iii) The graphical method can be used only when there are only $\qquad$ variables in a L.P.P.
(iv) A basic feasible solution is said to be $\qquad$ if values of all basic variables are non-zero and positive.
(v) What do you mean by unbounded solution?
(vi) Obtain dual of Maximize

$$
Z=2 x+5 y
$$

Subject to $\quad-x_{1}-x_{2} \leq 5$

$$
x_{1}-5 x_{2} \leq 4
$$

$$
x_{1}, x_{2} \geq 0
$$

2. (A) (i) Explain transportation problem and describe the North-West corner rule to obtain its initial basic feasible solution.
(ii) Solve the following transportation problem by Vogel's method and obtain optimal solution :

|  |  | Consumer |  |  | Available |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | B | C |  |  |
| Supplier | I | 6 | 8 | 4 | 14 |
|  | II | 4 | 9 | 8 | 12 |
|  | III | 1 | 2 | 6 | 5 |
| OR |  |  |  |  |  |
| Required |  |  |  |  | 6 |
| 10 | 15 | 32 |  |  |  |

(i) Explain :
(a) Unbalanced transportation problem
(b) Degeneracy in transportation problem.
(ii) The cost matrix of a transportation problem is given below. Solve it by North-West Corner rule and Least cost method.

|  | P | Q | R | S | Supply |
| :---: | :---: | :---: | :---: | :---: | :---: |
| A | 5 | 6 | 2 | 1 | 20 |
| B | 2 | 3 | 5 | 8 | 20 |
| C | 2 | 6 | 7 | 4 | 20 |
| Demand | 15 | 15 | 15 | 15 |  |

(B) Answer the following: (any four)
(i) What do you mean by balanced transportation problem?
(ii) If total supply $\qquad$ total demand then dummy column is added to make it balance.
(iii) $\quad \Delta_{\mathrm{ij}}=\mathrm{C}_{\mathrm{ij}}-$ $\qquad$
(iv) How many methods are used to solve transportation problem?
(v) Full form of V.A.M. is $\qquad$ .
(vi) If all values of $\Delta_{\mathrm{ij}}>0$, the solution is $\qquad$ and $\qquad$ .
3. (A) (i) Give difference between PERT and CPM.
(ii) Find EST, LST, EFT, LFT and total float for each activity.

| Activity | $1-2$ | $1-3$ | $2-4$ | $3-4$ | $3-5$ | $4-5$ | $4-6$ | $5-6$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Time | 6 | 5 | 10 | 3 | 4 | 6 | 2 | 9 |
| OR |  |  |  |  |  |  |  |  |

(i) Give the advantages and limitations of PERT.
(ii) Time estimates and predecessor of each activity in a project are given below. Find Free Float for each activity.

| Activity | A | B | C | D | E | F | G | H |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Immediate <br> Predecessor | - | - | - | C | A, B | E, D | D | F, G |
| Time (in days) | 4 | 6 | 8 | 4 | 8 | 4 | 3 | 3 |

(B) Answer the following: (any three)
(i) Define Pessimistic Time.
(ii) CPM was developed by $\qquad$ .
(iii) Define EST.
(iv) The optimistic time is denoted by $\qquad$ .
(v) Prepare a PERT chart for the following project :

| Activity | $1-2$ | $2-3$ | $2-4$ | $3-4$ | $3-5$ | $4-5$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Time | 2 | 3 | 1 | 2 | 3 | 5 |

4. (A) (i) What is Game Problem ? What are the assumptions made in Game theory ?
(ii) A company has 4 machines on which to do 3 jobs. Each job can be assigned to one and only one machine. The cost of each job on each machine is given in the following table. What are the job assignments for minimum cost ?

|  |  | Machine |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | W | X | Y | Z |
| Job | A | 17 | 23 | 27 | 31 |
|  | B | 7 | 12 | 16 | 18 |
|  | C | 9 | 14 | 1 | 21 |

(i) Solve the following game :

$$
\begin{gathered}
\mathrm{y} \\
x\left[\begin{array}{ll}
4 & 1 \\
2 & 3
\end{array}\right]
\end{gathered}
$$

(ii) Solve the following assignment problem for minimum cost :

|  | A | B | C | $\mathbf{D}$ |
| :---: | :---: | :---: | :---: | :---: |
| I | 1 | 4 | 6 | 3 |
| II | 9 | 7 | 10 | 9 |
| III | 4 | 5 | 11 | 7 |
| IV | 8 | 7 | 8 | 5 |

(B) Answer the following : (any three)

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(i) The method used for solving an assignment problem is called $\qquad$ .
(ii) The competitor are called $\qquad$ .
(iii) What is saddle point?
(iv) What do you mean by unbalance assignment problem?
(v) The objective of assignment problem is to assign number of origins to equal number of destinations at a maximum cost or at a minimum profit.
(True/False)

